

# Reactivity Measurements in MUSE-4 Using Noise Analysis Techniques

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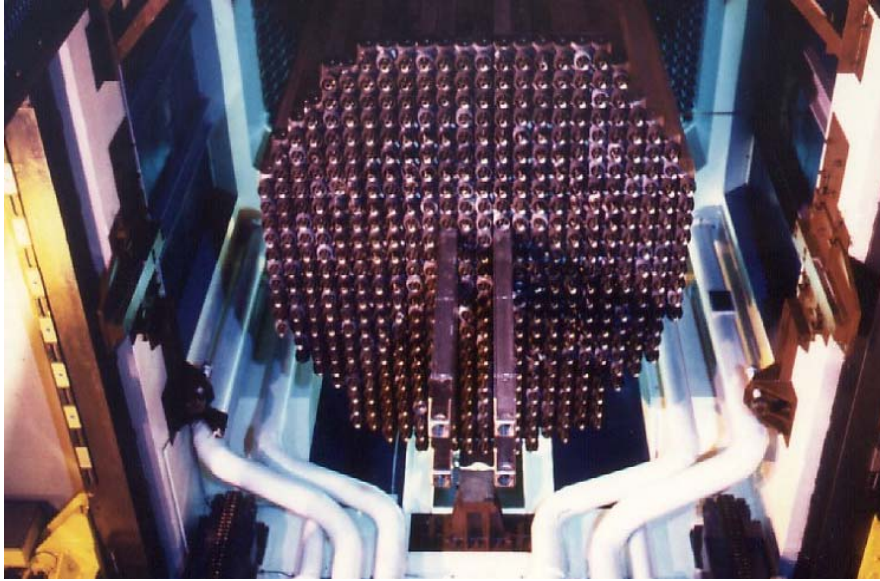
**In cooperation with CEA, CNRS, and other MUSE partners**

# MUSE-4 Project

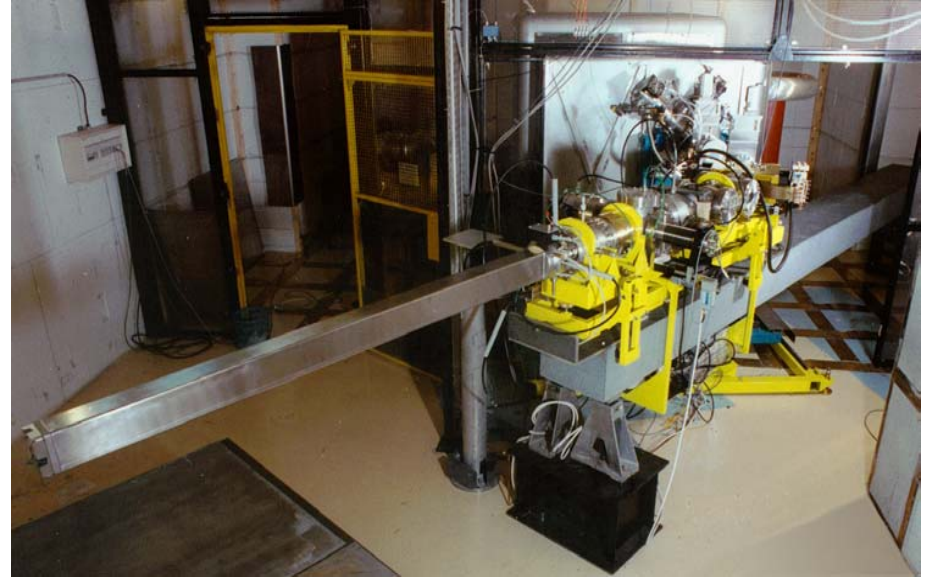
## Objectives:

- Understanding of the behavior of a subcritical reactor core driven by an external neutron source
- Development of experimental techniques for the control and the monitoring of a future ADS
- Definition of reference tools (nuclear data, codes, ...)
- Follow-up of MUSE-3 (1998) that used a commercial neutron generator (14 MeV,  $2 \cdot 10^8$  n/s) in four configurations (critical, -500, -1000, -1500 pcm)
- Located at CEA, Cadarache (F)

# MUSE-4 Project



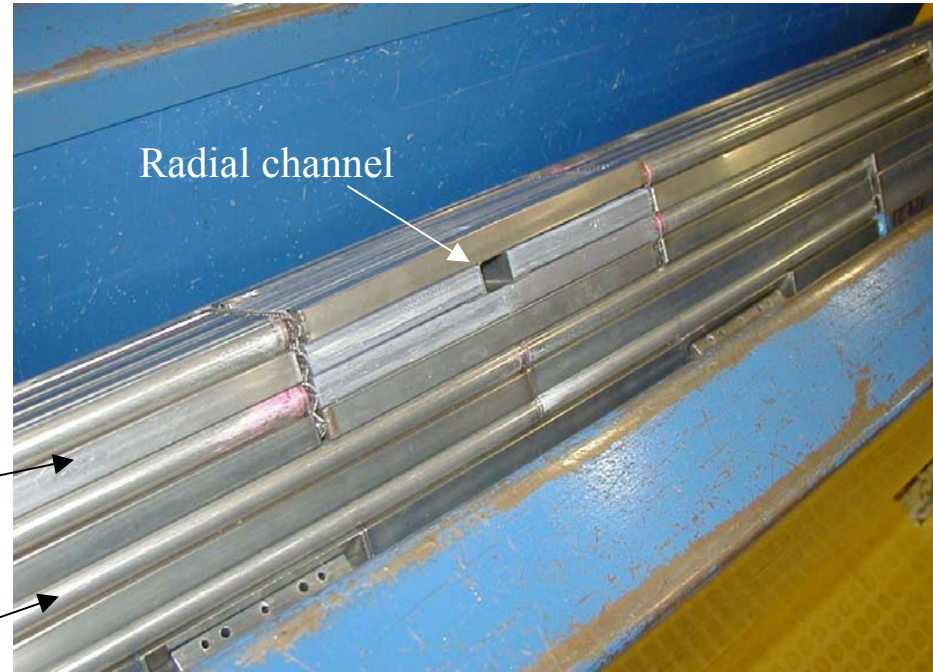
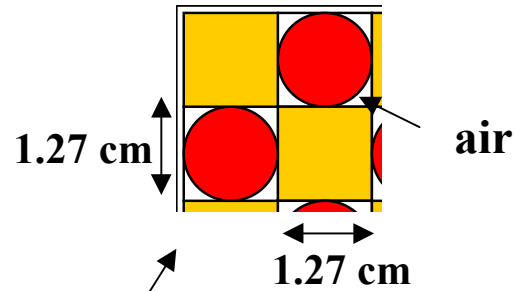
MASURCA core



GENEPI tube

# MASURCA Fuel

Tube thickness = 2.2



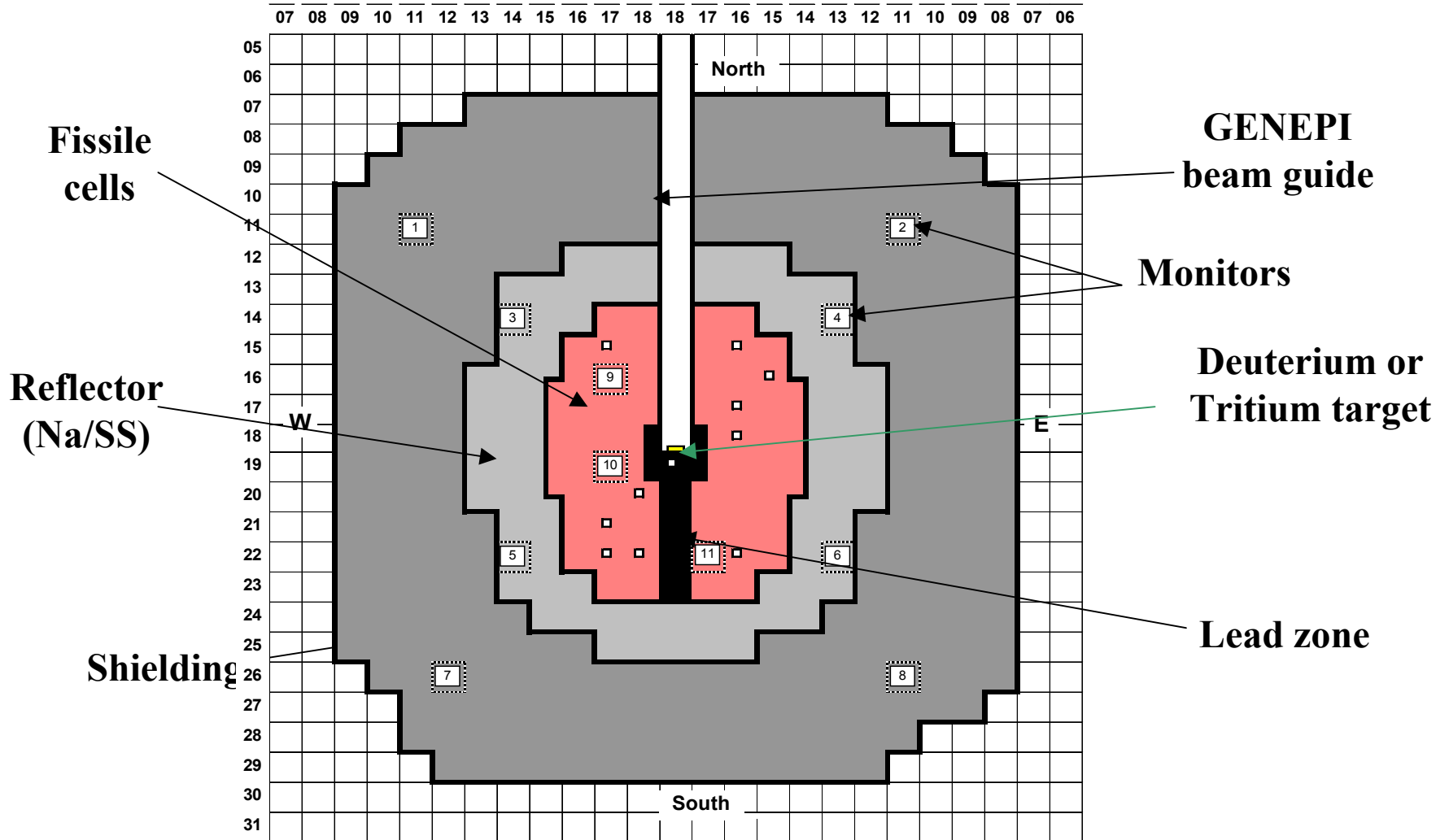
Na  
rodlet

PuO<sub>2</sub> rodlet

- 25% Pu
- <sup>240</sup>Pu/Pu = 18%

10,6 cm

# MASURCA Core



# GENEPI Accelerator

- Designed and made by CNRS, Grenoble
- D-D reaction ( $\sim 1.2 \cdot 10^8$  n/s at 4 kHz) or D-T ( $\sim 1.2 \cdot 10^{10}$  n/s)
- Pulse duration  $< 1 \mu\text{s}$

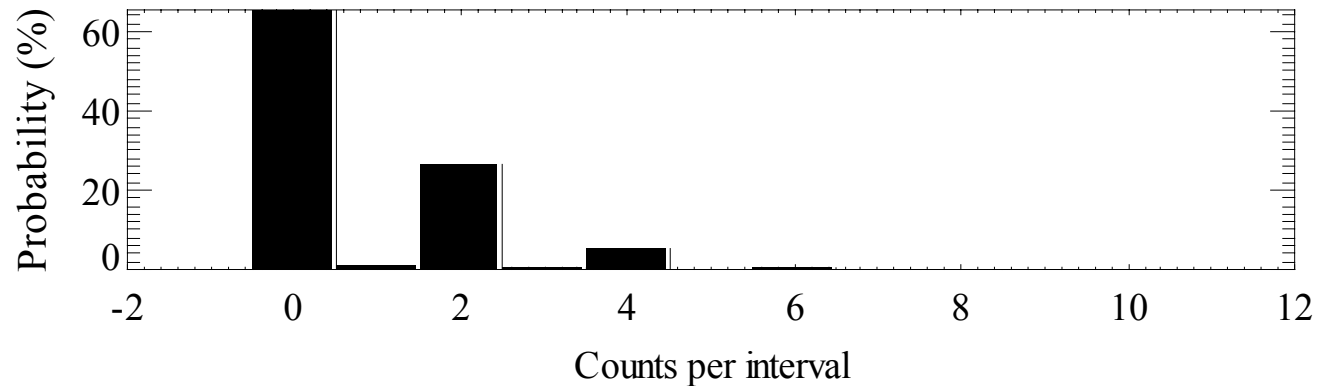
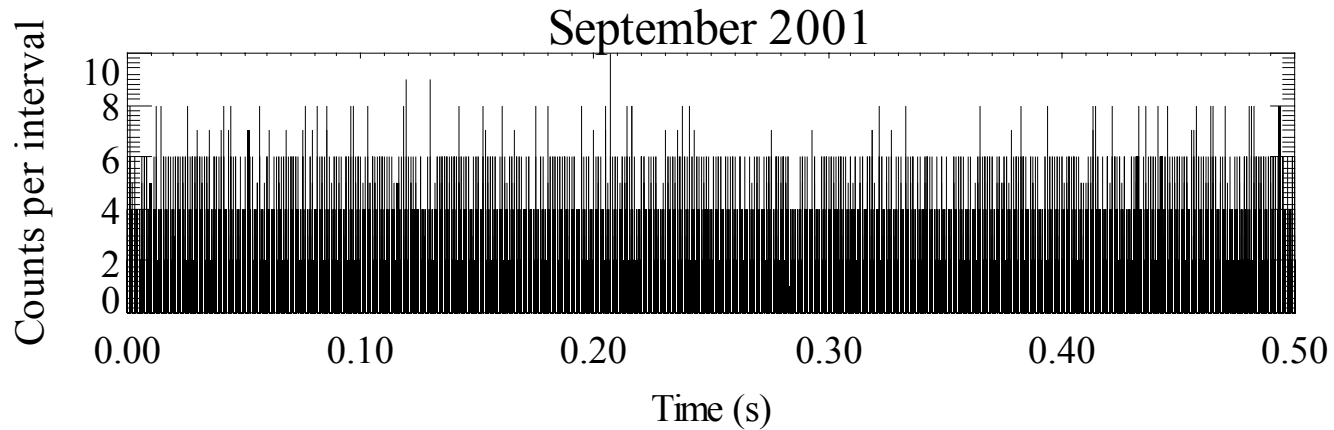
Beam energy (keV)	140 to 240 keV
Peak current (mA)	50
Repetition rate (Hz)	10 to 5 000
Minimum pulse duration ( $10^{-9}$ s)	700
Mean beam current ( $\mu\text{A}$ )	200 (for a duty cycle of 5 000 Hz)
Pulses reproducibility	Fluctuations at 1% level

# Measurements done by TU-Delft

- Pulse counting measurements (Feynman- $\alpha$ , correlation)
- Continuous current measurements (Transfer function)
- Rod drop measurements (PHYSOR-2002)

# Feynman- $\alpha$ results critical

Counts and echoes!



# Feynman- $\alpha$ results critical

Pattern	0000	0100	0010	0200	0020	0110
Number	3795830	418	435	1543291	1543460	36306

From the fraction 0110 counts, the delay between each neutron detection and its echo can be extracted:  $d=115$  ns

$$Y' = \frac{\sigma^2}{\mu} - 2 + \frac{d}{T} = Y - 1 + \frac{d}{T}.$$

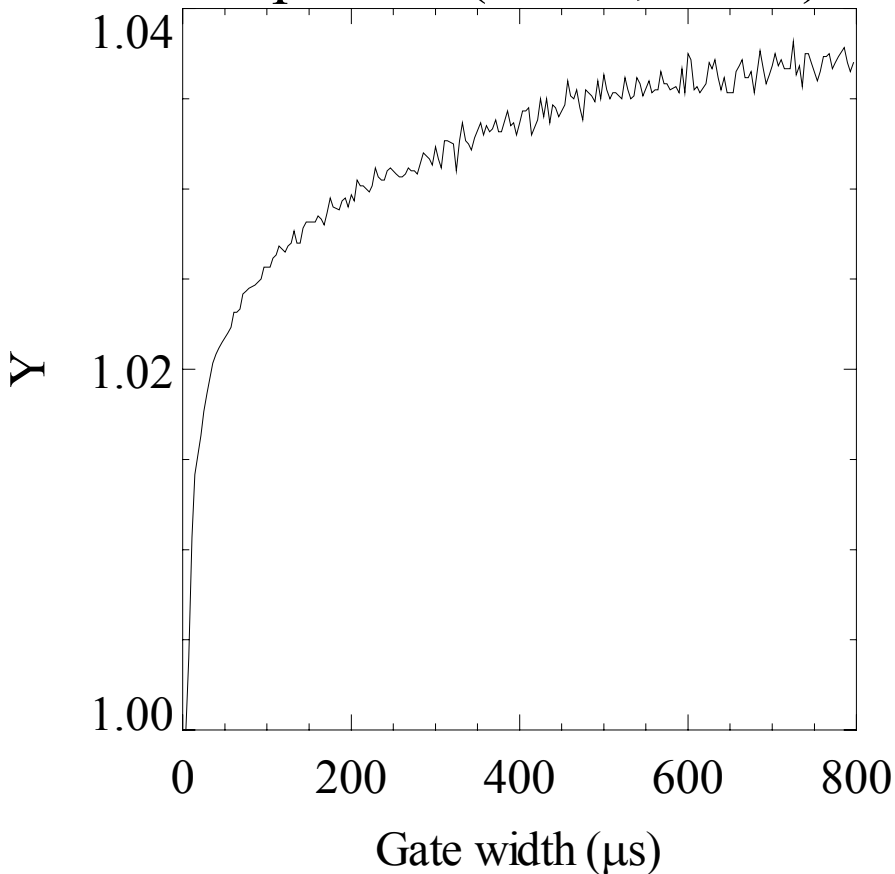
$Y$  = correlated part in variance-to-mean

$Y'$  = corrected correlated part in var-to-mean

# Feynman- $\alpha$ results critical

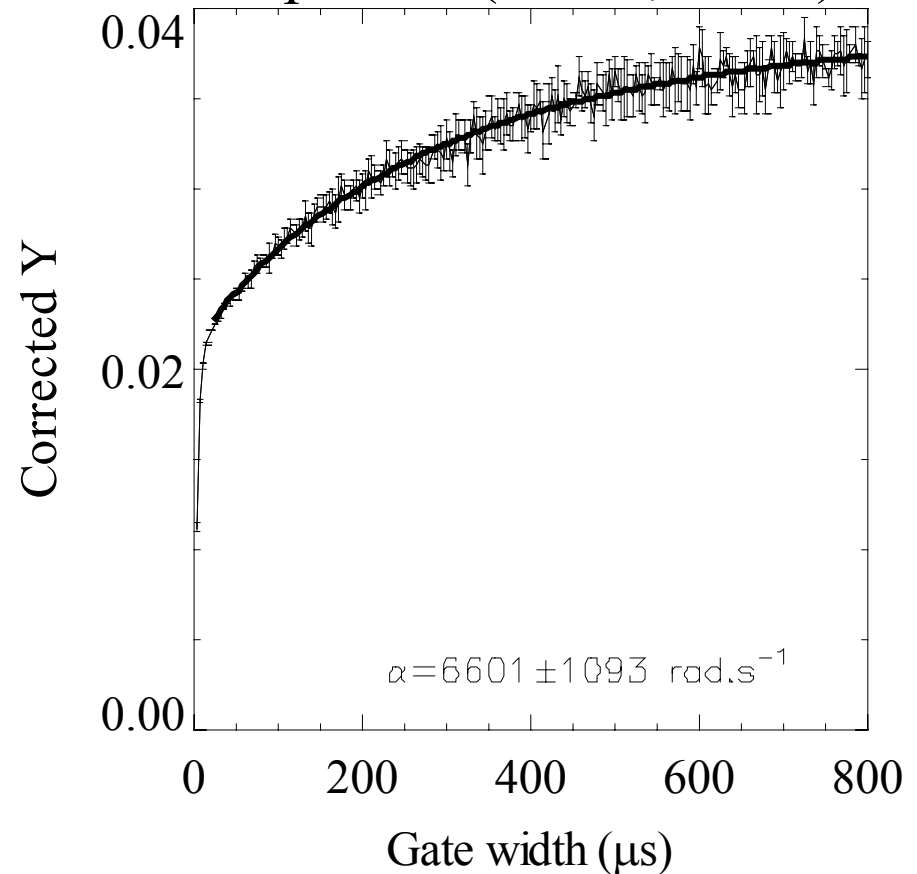
Original

Sep 2001 (Det B, 20 W)



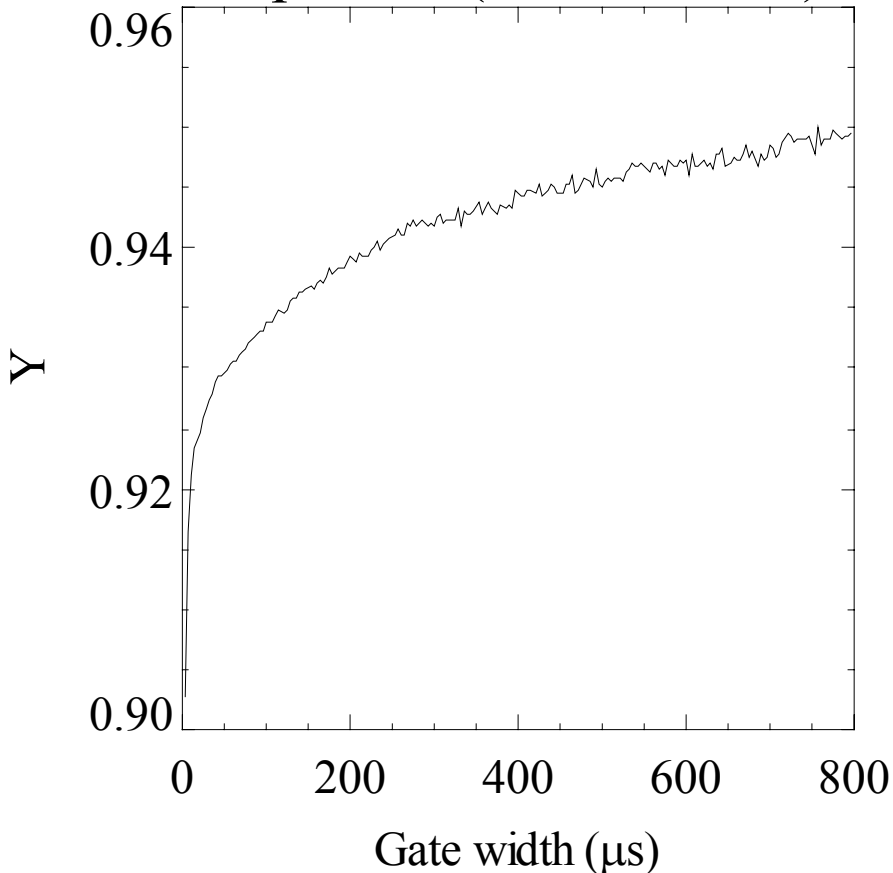
Corrected

Sep 2001 (Det D, 20 W)

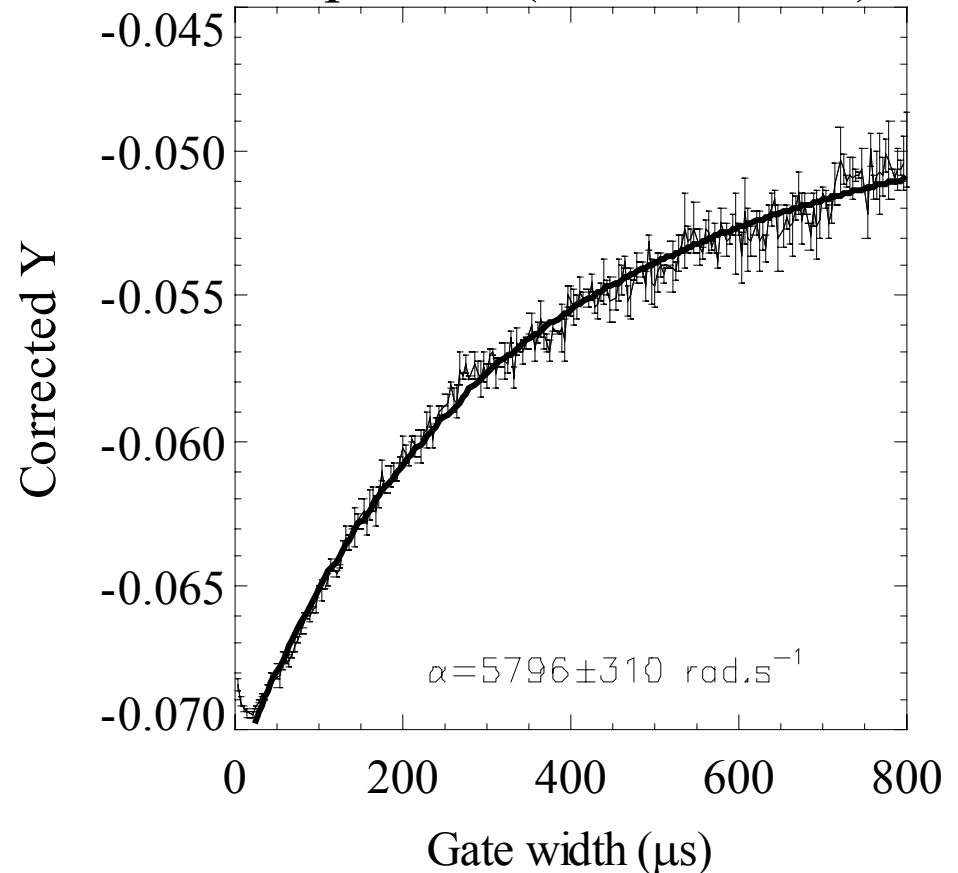


# Feynman- $\alpha$ results critical

Original  
Sep 2001 (Det D, 20 W)

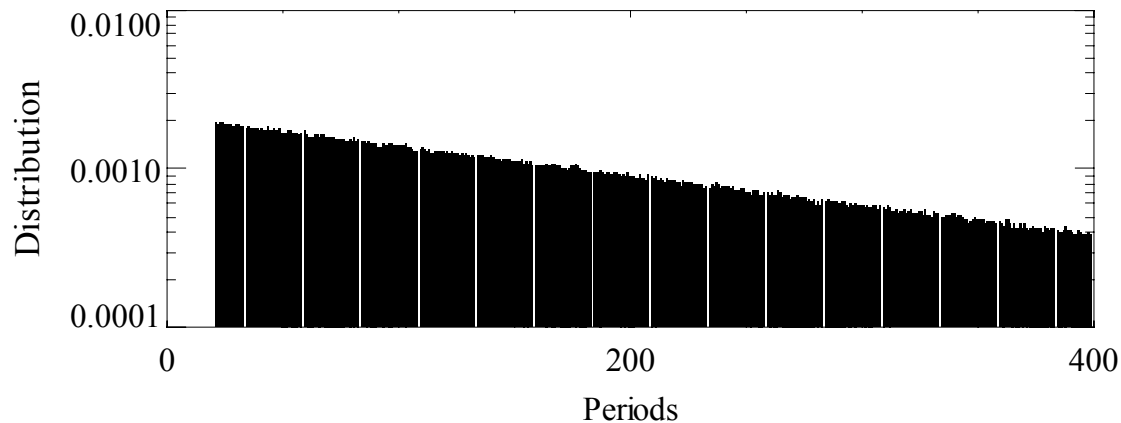
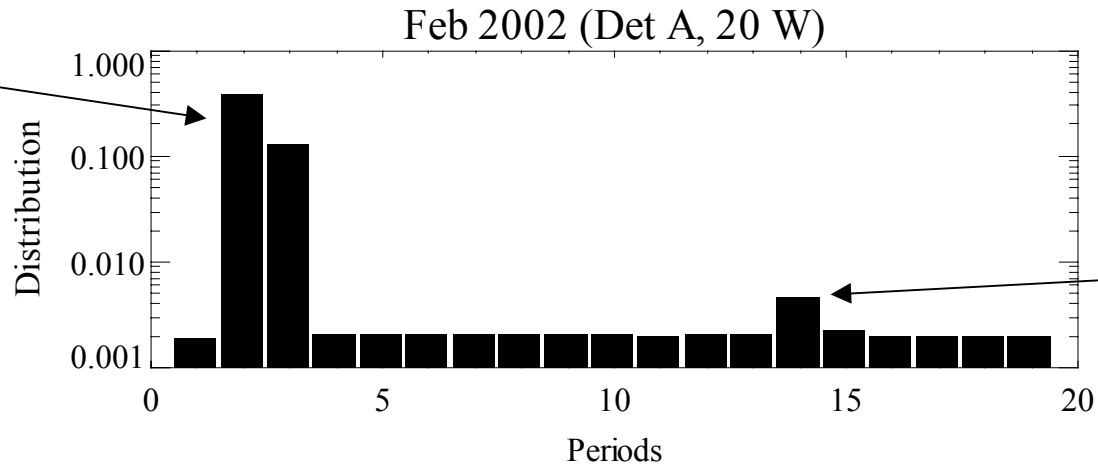


Corrected  
Sep 2001 (Det D, 20 W)



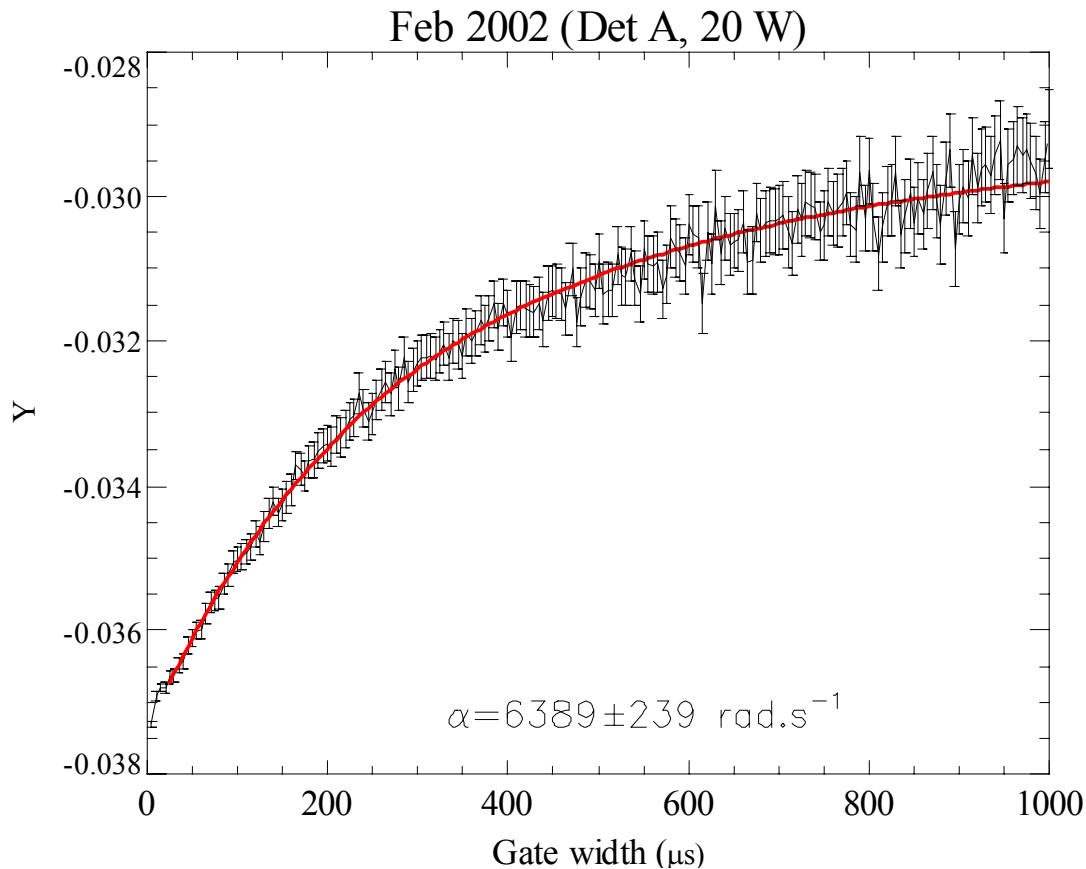
# Feynman- $\alpha$ results critical

Echoes at  
 $\approx 115$  ns

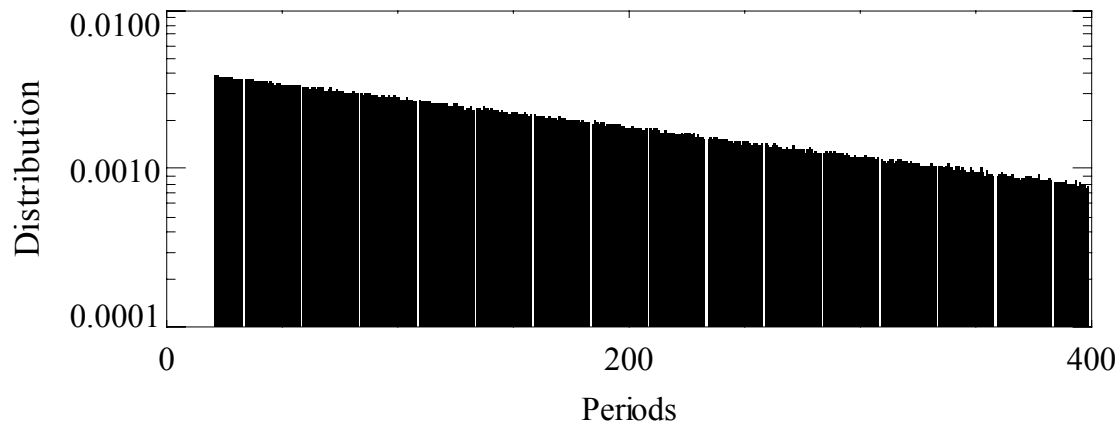
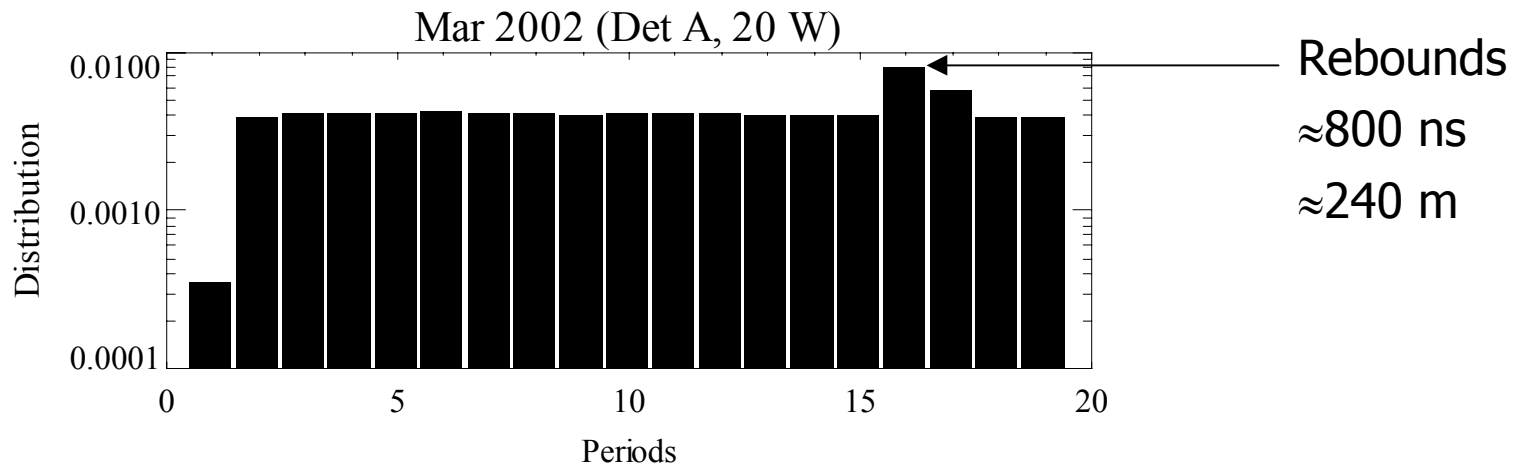


# Feynman- $\alpha$ results critical

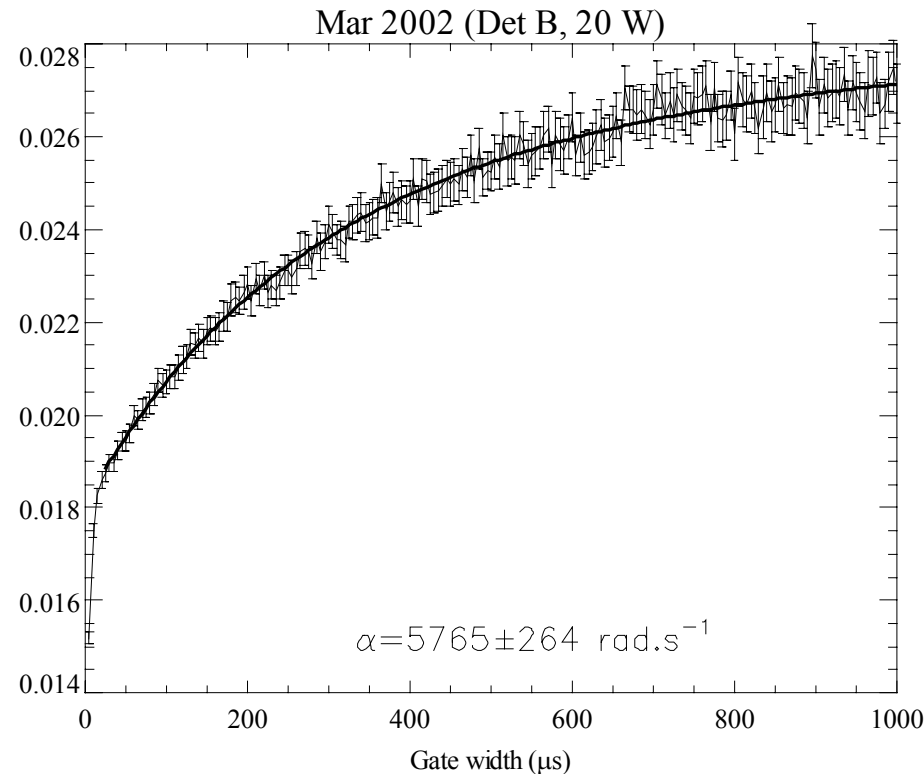
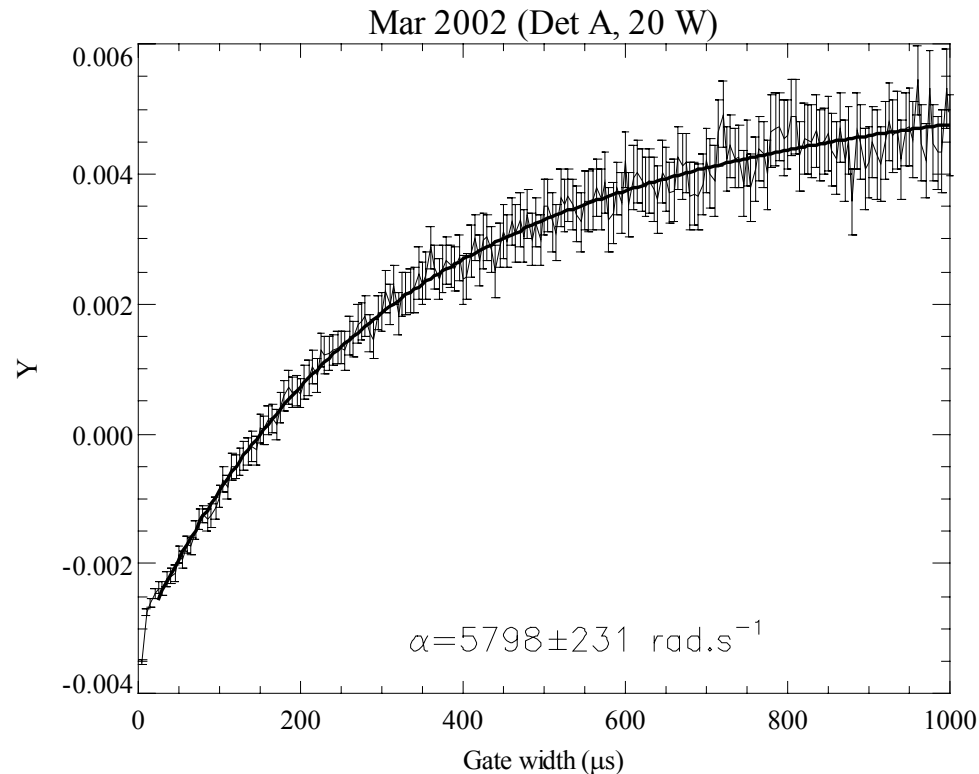
Other measurement method: counts between pulses  
All echoes removed within 200 ns after each detection



# Feynman- $\alpha$ results critical

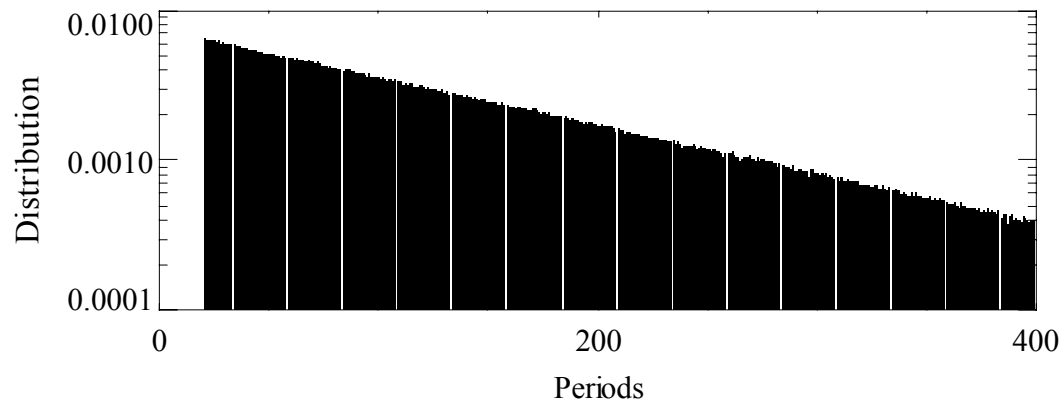
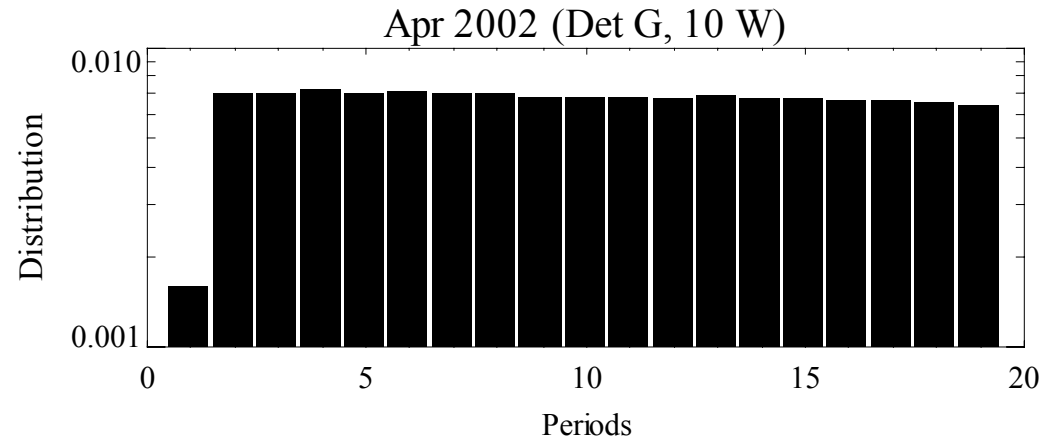


# Feynman- $\alpha$ results critical



Calculations:  $\beta=335 \text{ pcm}$ ,  $\Lambda=0.586 \mu\text{s}$ ,  $\alpha\approx 5720 \text{ s}^{-1}$

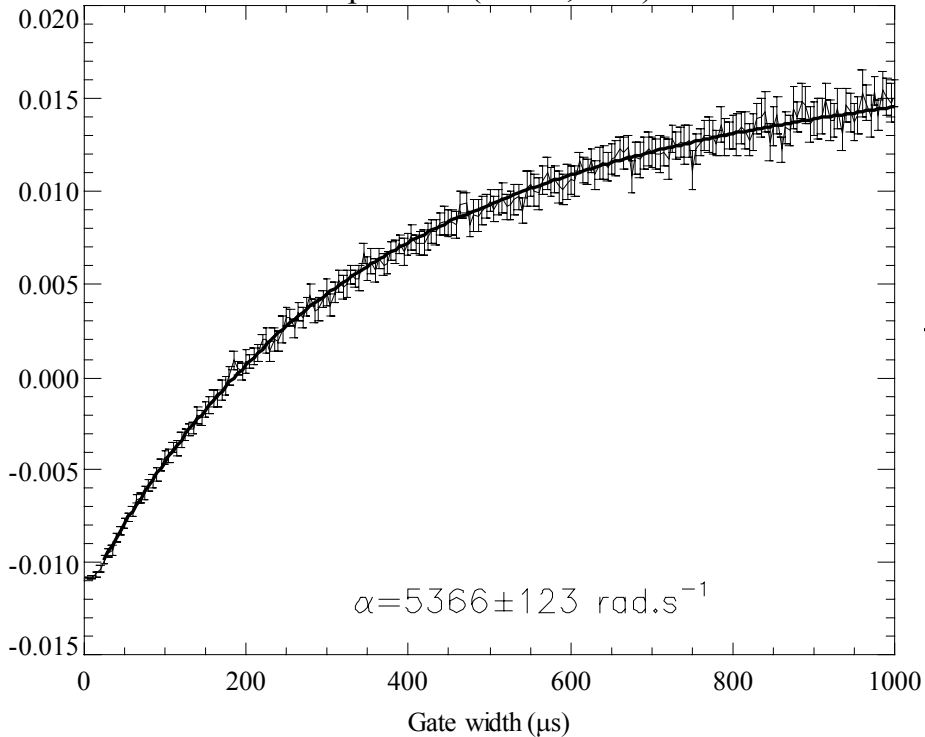
# Feynman- $\alpha$ results critical



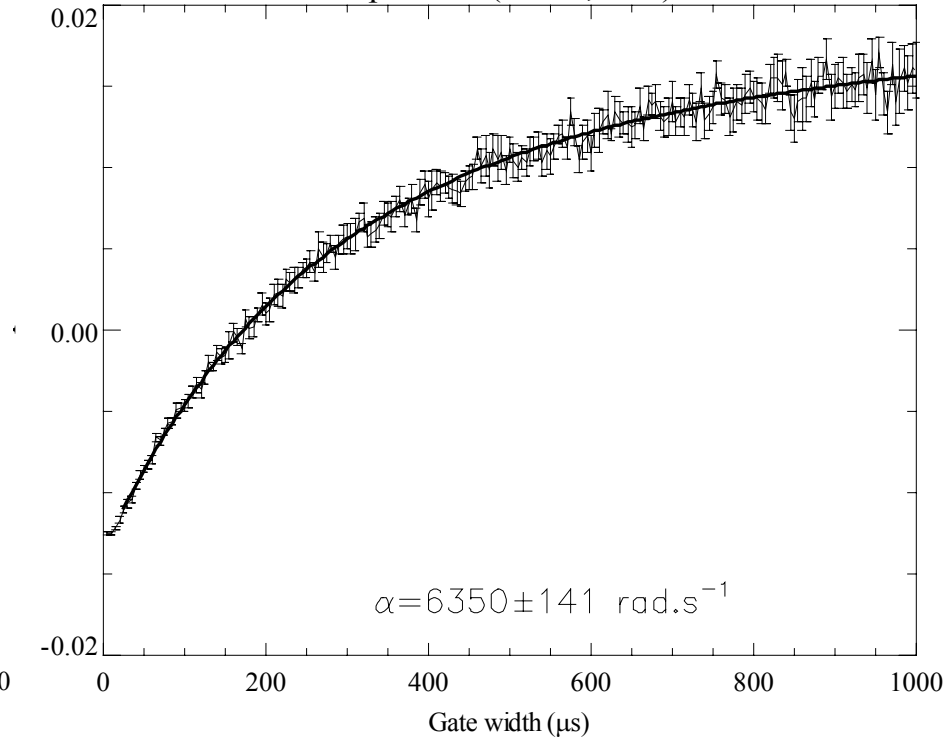
# Feynman- $\alpha$ results critical

Reactor power 5 W

Apr 2002 (Det G, 5 W)

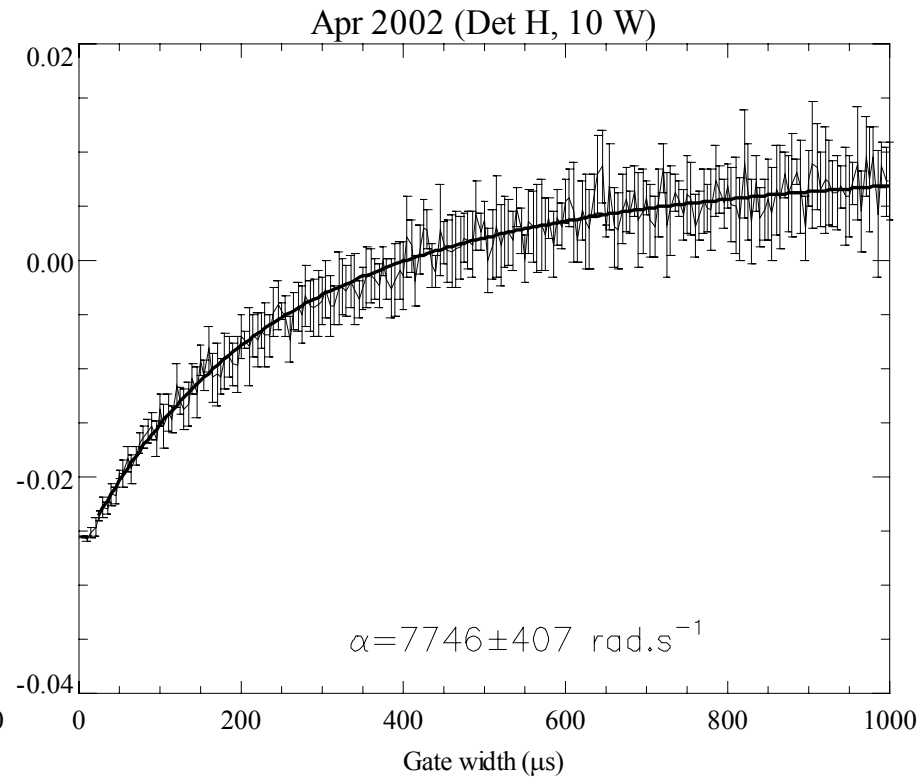
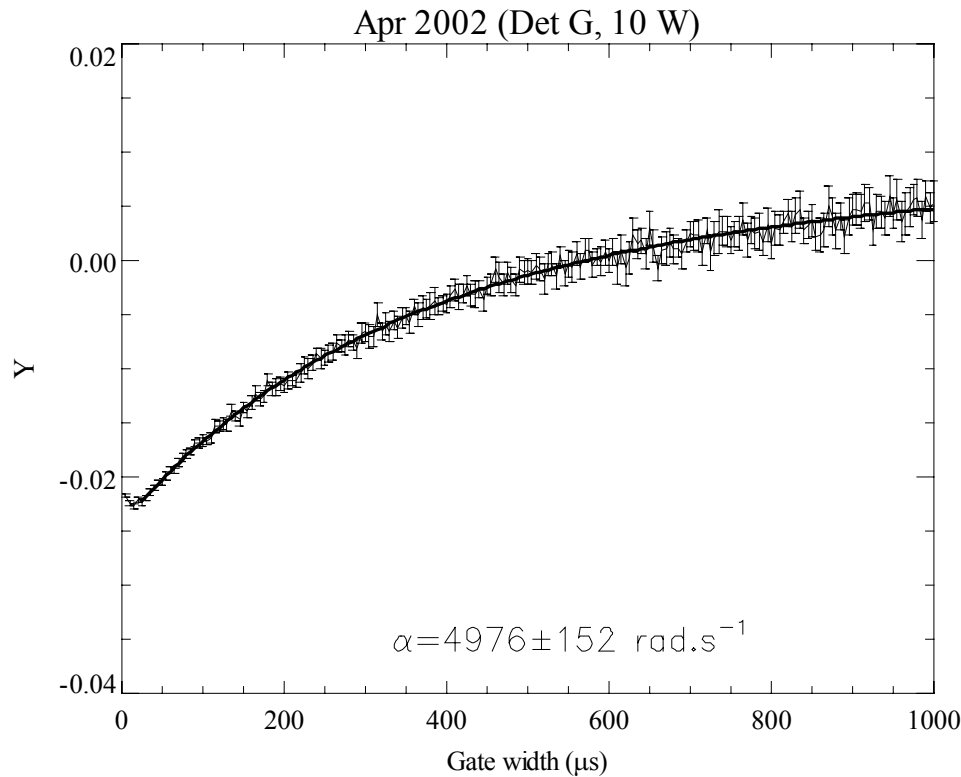


Apr 2002 (Det H, 5 W)



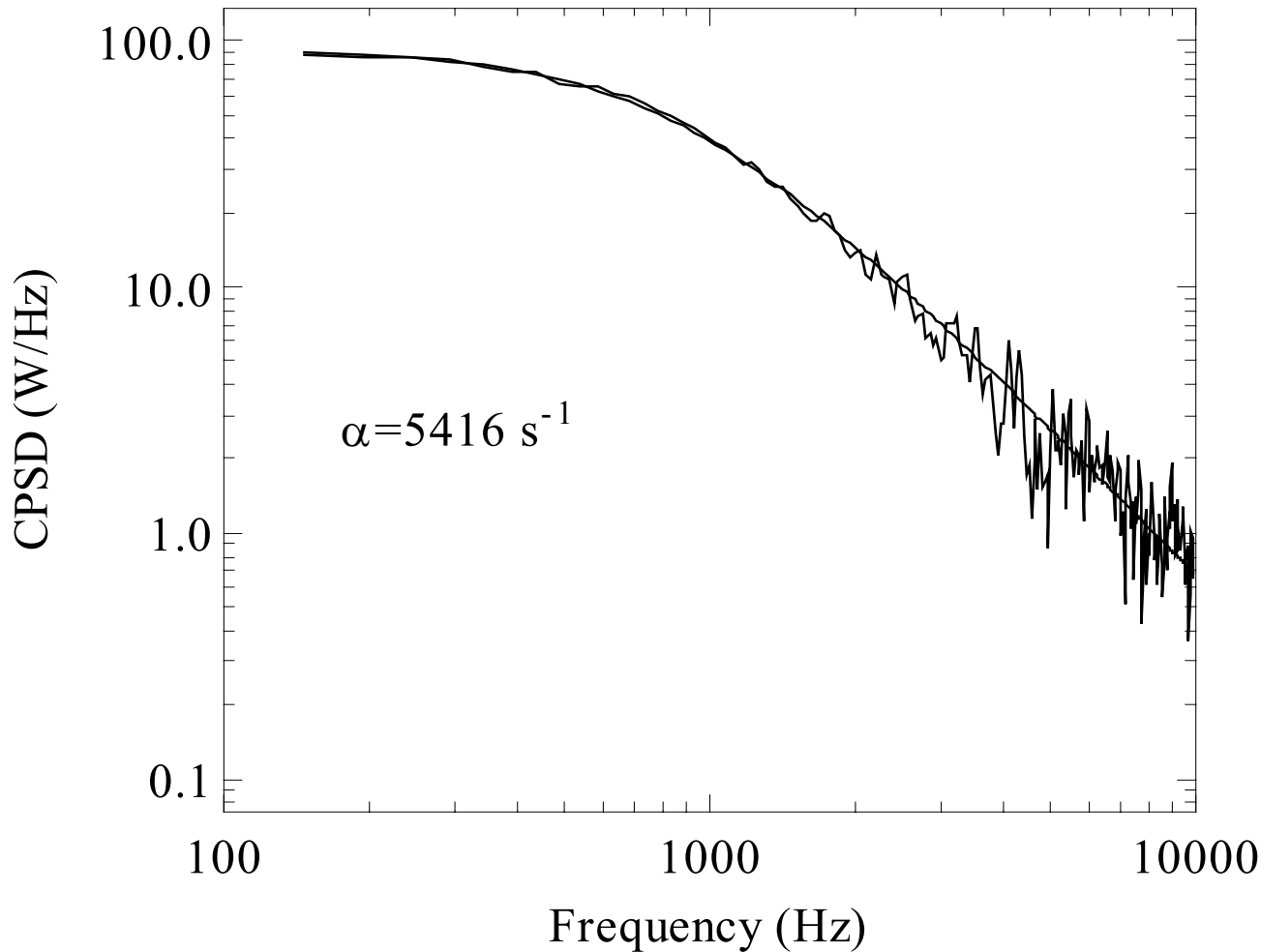
# Feynman- $\alpha$ results critical

Reactor power 10 W



# CPSD results critical

Det A-B



Calculations:

- $\beta = 335 \text{ pcm}$
- $\Lambda = 0.586 \text{ } \mu\text{s}$
- $\alpha \approx 5720 \text{ s}^{-1}$

# Feynman- $\alpha$ pulsed subcritical systems

Pazsit et al (PHYSOR 2002),

Yamana et al (PHYSOR 2002),

Kitamura et al (ANE, **38**, 879-909):

Stochastically pulsed system:

$$Y(T) = \frac{\sigma^2(T)}{\mu(T)} - 1 = \frac{2\varepsilon S_0 T_p^5 \alpha}{T \pi^4} \sum_{n=0}^{\infty} \frac{1}{4n^6 \pi^2 + n^4 \alpha^2 T_p^2} \sin^2\left(\frac{\pi n \tau}{T_p}\right) + \frac{\varepsilon \lambda_f \overline{\nu(\nu-1)}}{\alpha^2} \left(1 - \frac{1 - e^{-\alpha T}}{\alpha T}\right)$$

Deterministically pulsed system:

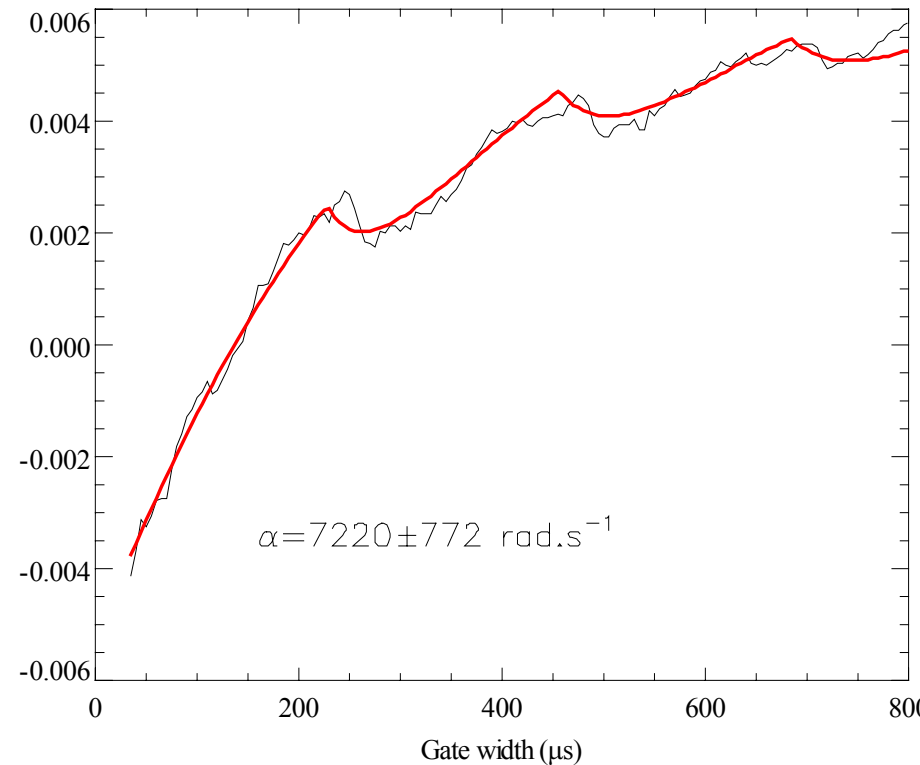
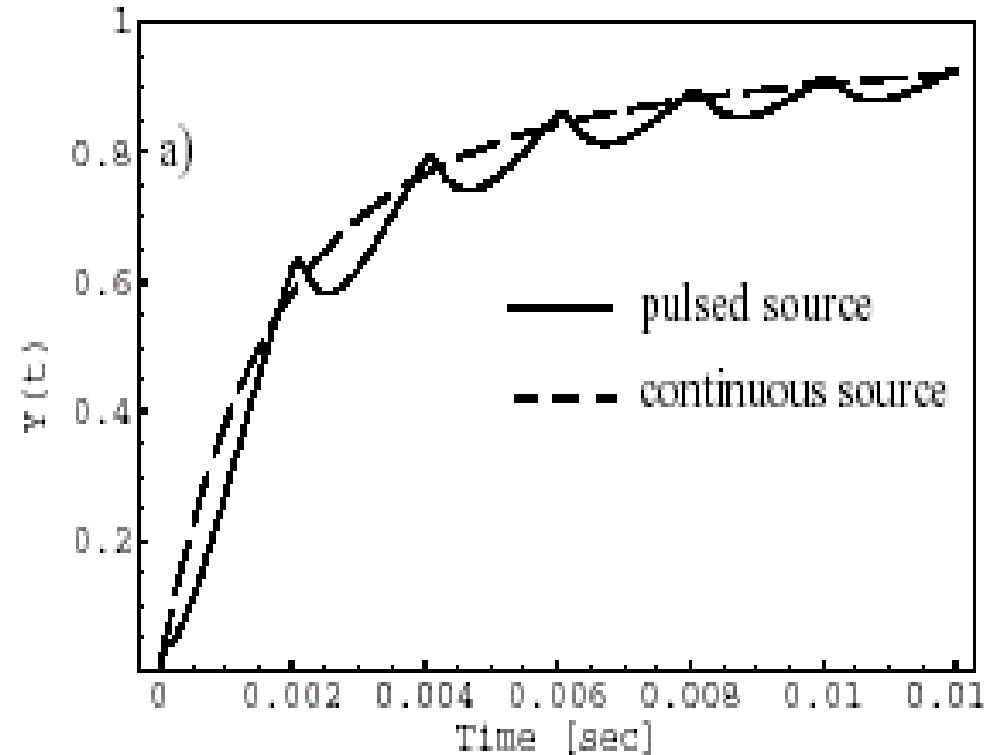
$$Y(T) = \frac{\lambda_d \lambda_f \langle \nu(\nu-1) \rangle}{\alpha^2} \frac{\left\{ \begin{aligned} &2\Delta_{\alpha\tau}(1 - e^{-\alpha T} - \alpha T e^{-\alpha T}) + \Delta_{2\alpha\tau}(\delta - 1)(1 - e^{-\alpha T})^2 \\ &+ \sum_{m=1}^M \left[ 2\{1 - e^{-\alpha(T-m\tau)} - \alpha(T-m\tau)e^{-\alpha(T-m\tau)}\} \right] \\ &+ (\delta = 1)\{1 - e^{-\alpha(T-m\tau)}\}^2 \end{aligned} \right\}}{\Delta_{\alpha\tau}(1 - e^{-\alpha T}) + \sum_{m=1}^M \{1 - e^{-\alpha(T-m\tau)}\}}$$

# Feynman- $\alpha$ results subcritical

Deterministically pulsed system; D-D @ 4.4 kHz

Theory (I. Pazsit)

Experiment (D-D)



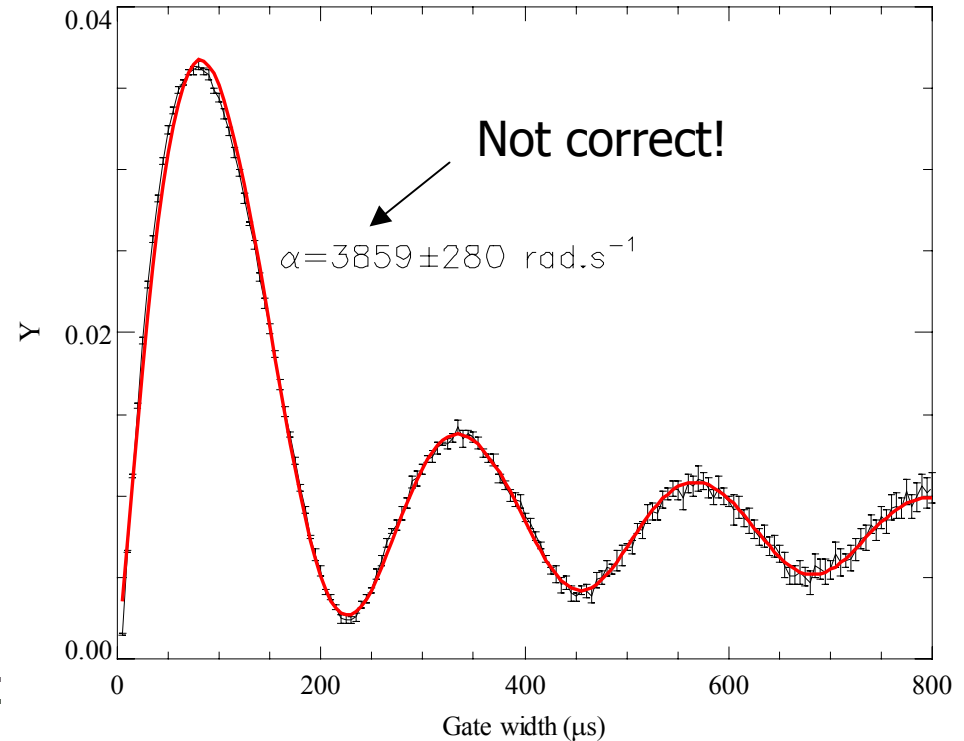
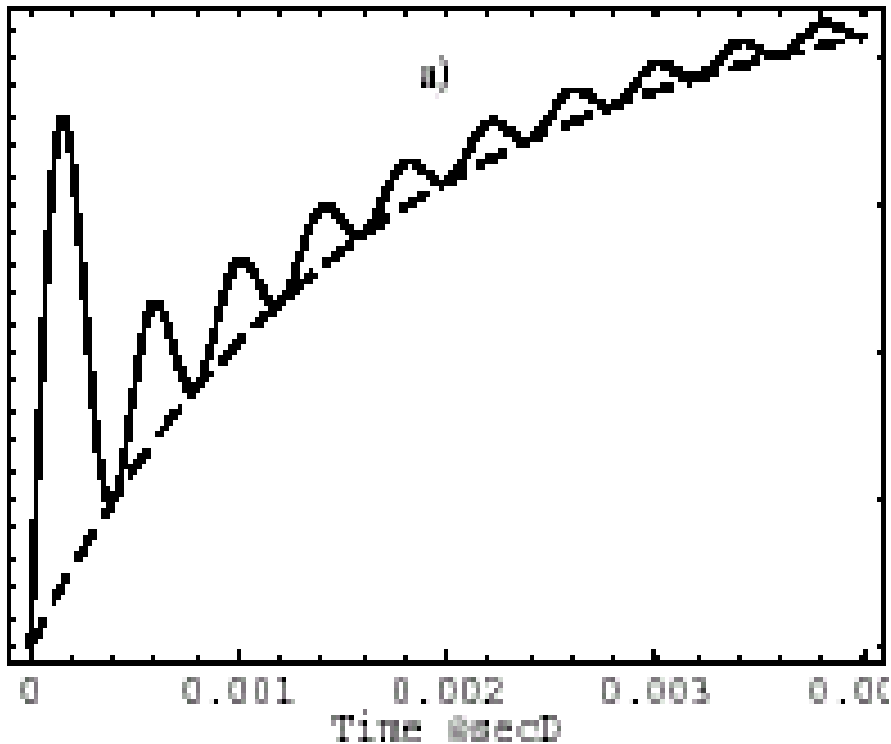
# Feynman- $\alpha$ results subcritical

Stochastically pulsed system; D-D @ 4.4 kHz

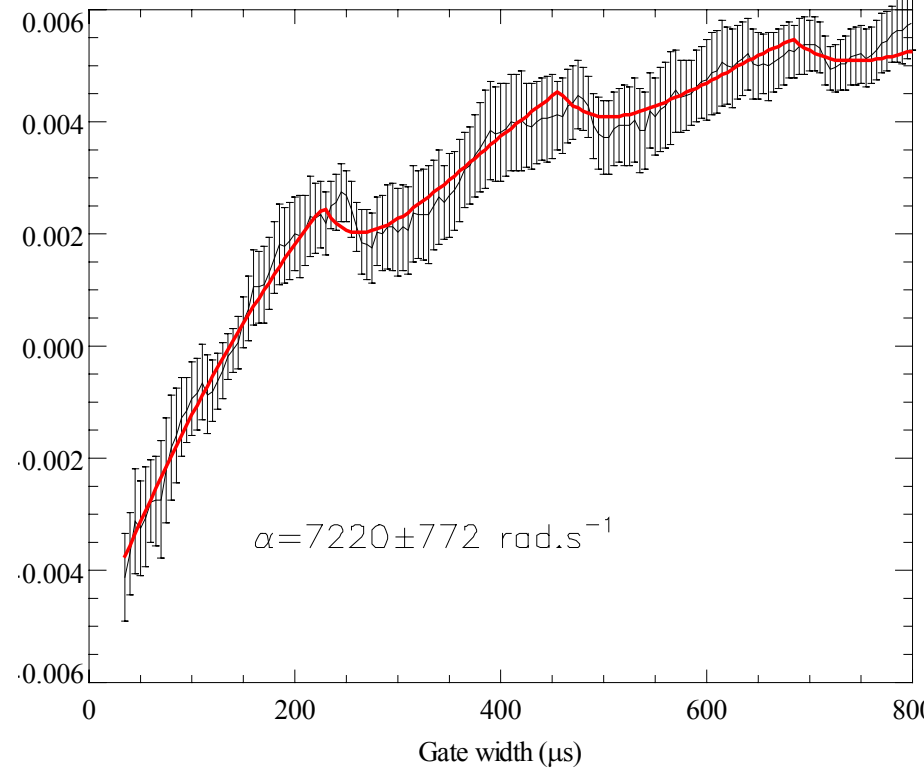
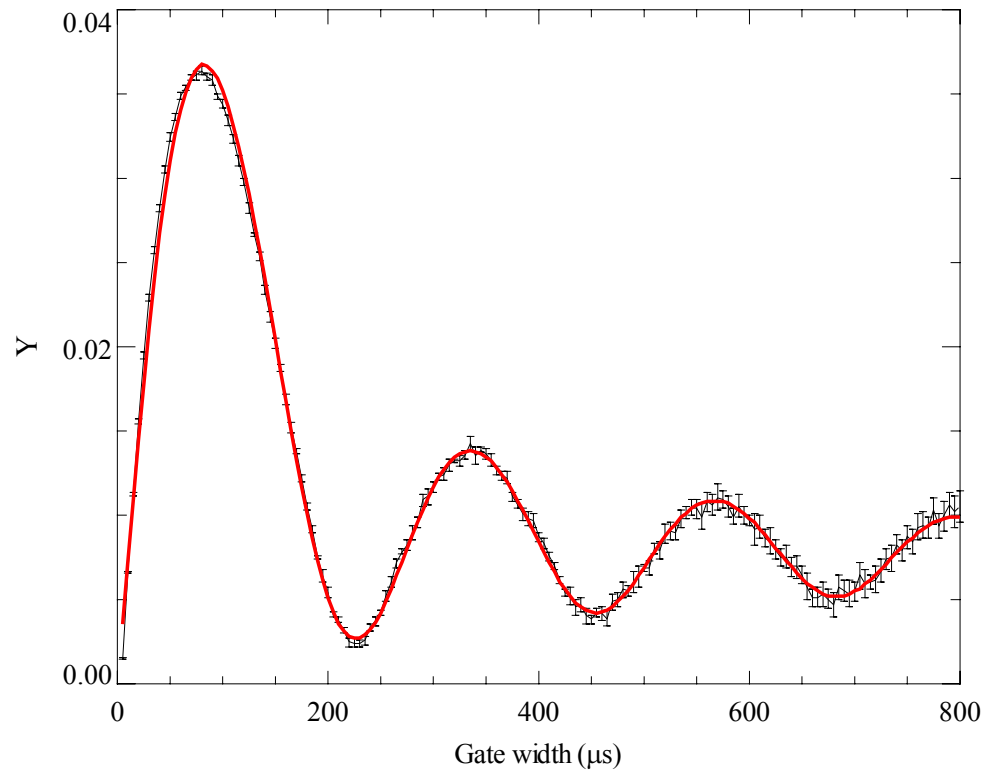
Theory (I. Pazsit)

Experiment (D-D)

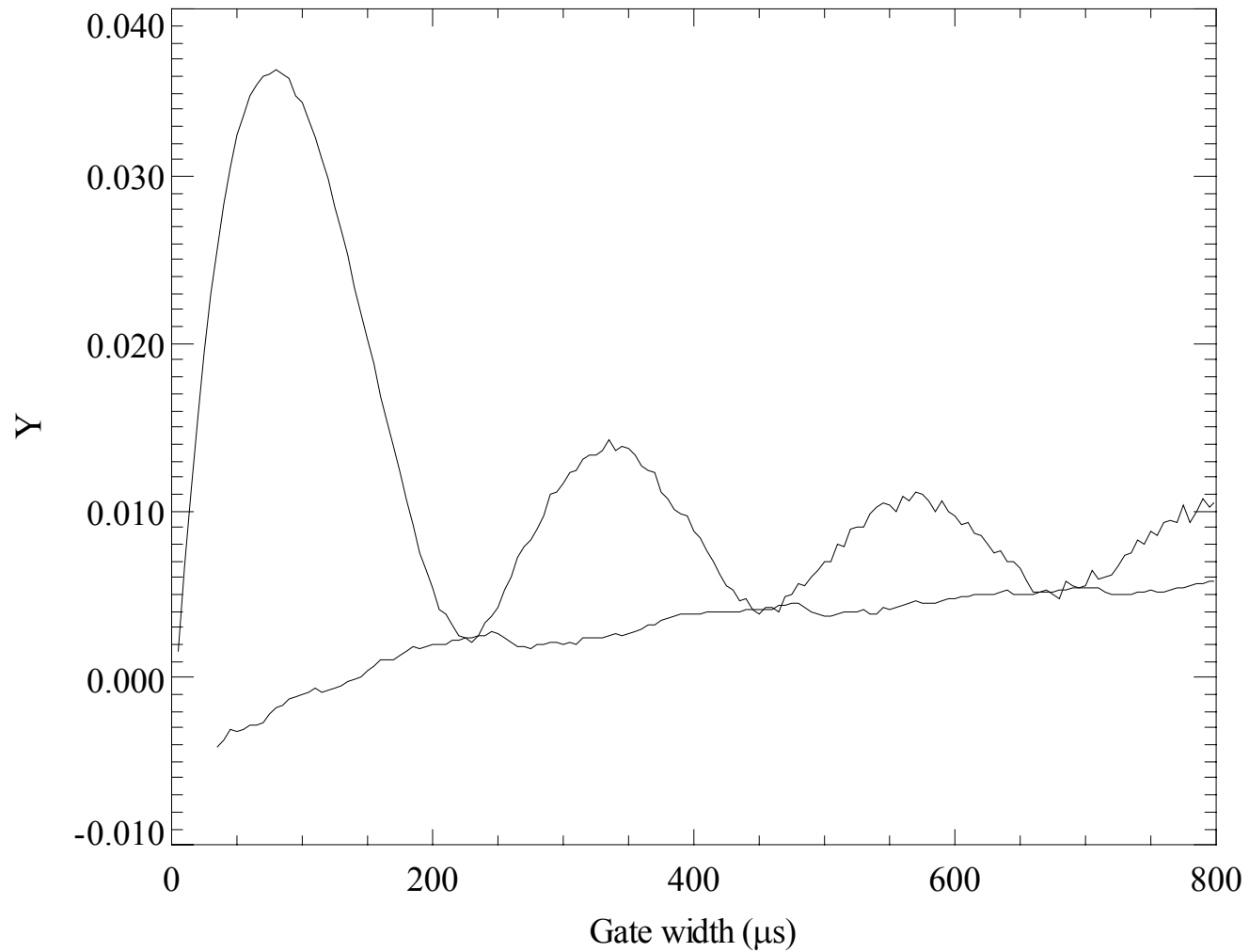
Stochastic



# Feynman- $\alpha$ results subcritical

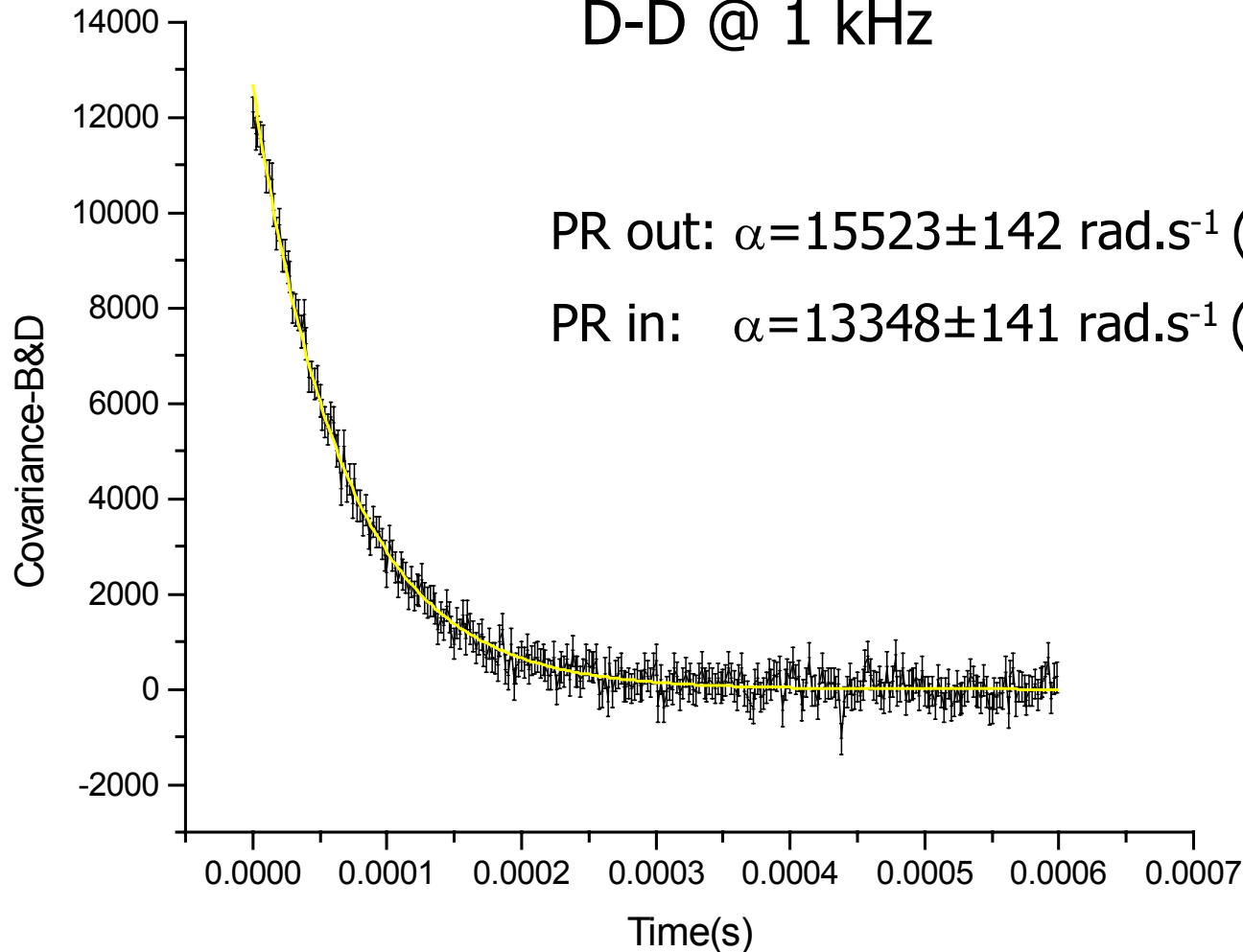


# Feynman- $\alpha$ results subcritical



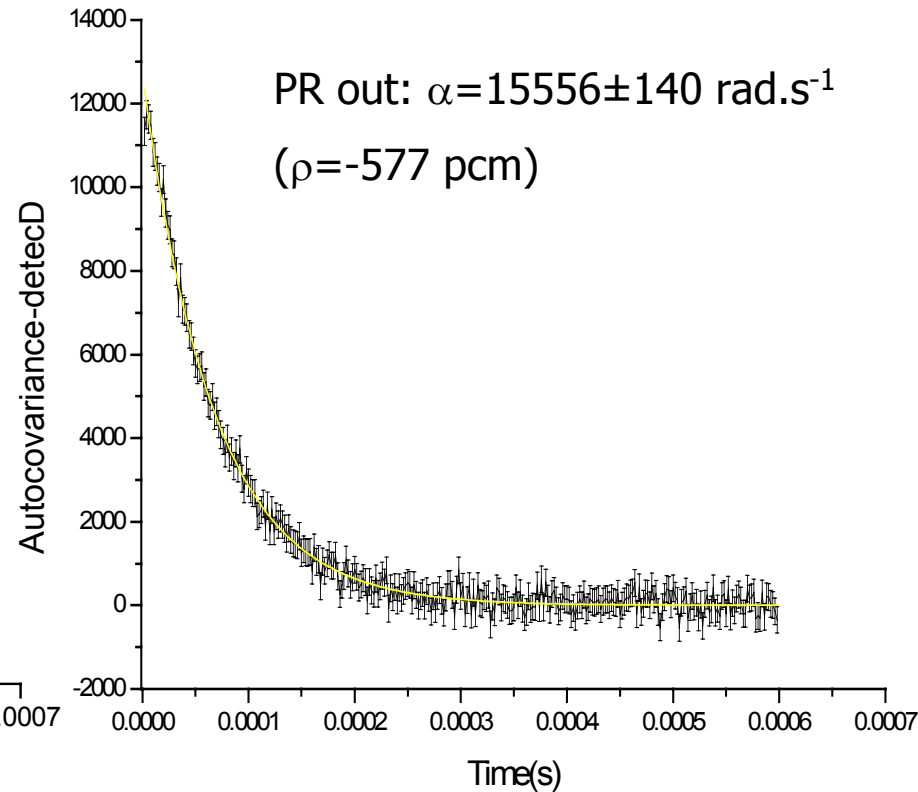
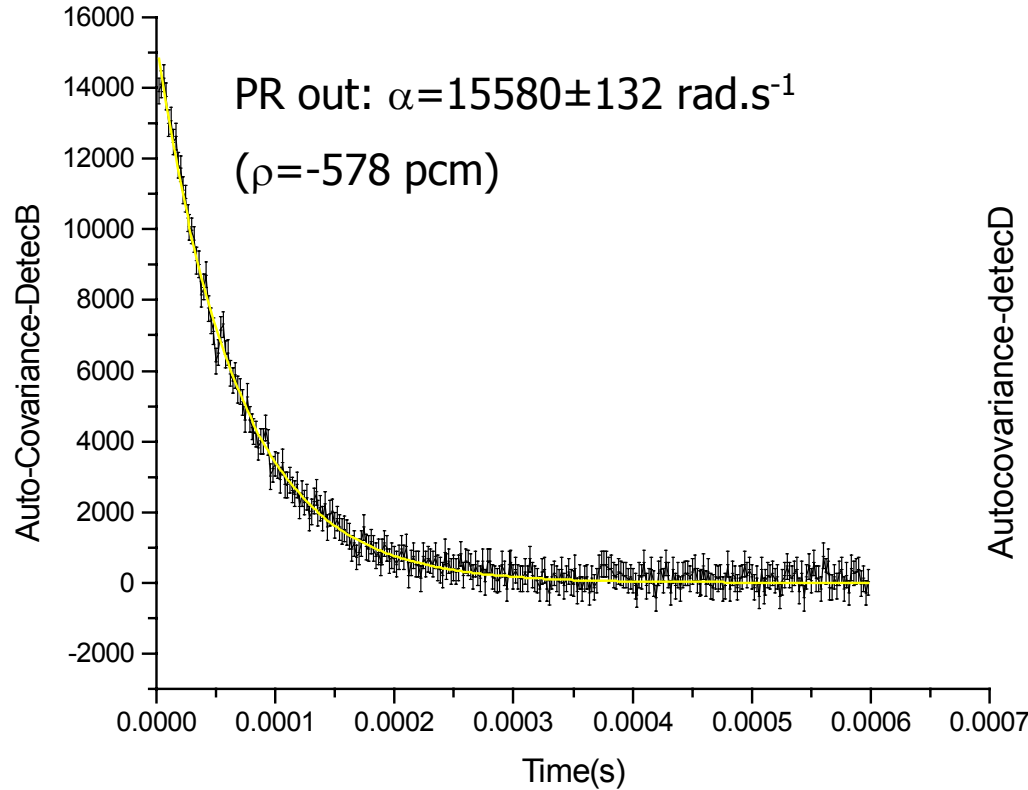
# Correlation results $\approx 1.5\%$ subcritical

D-D @ 1 kHz

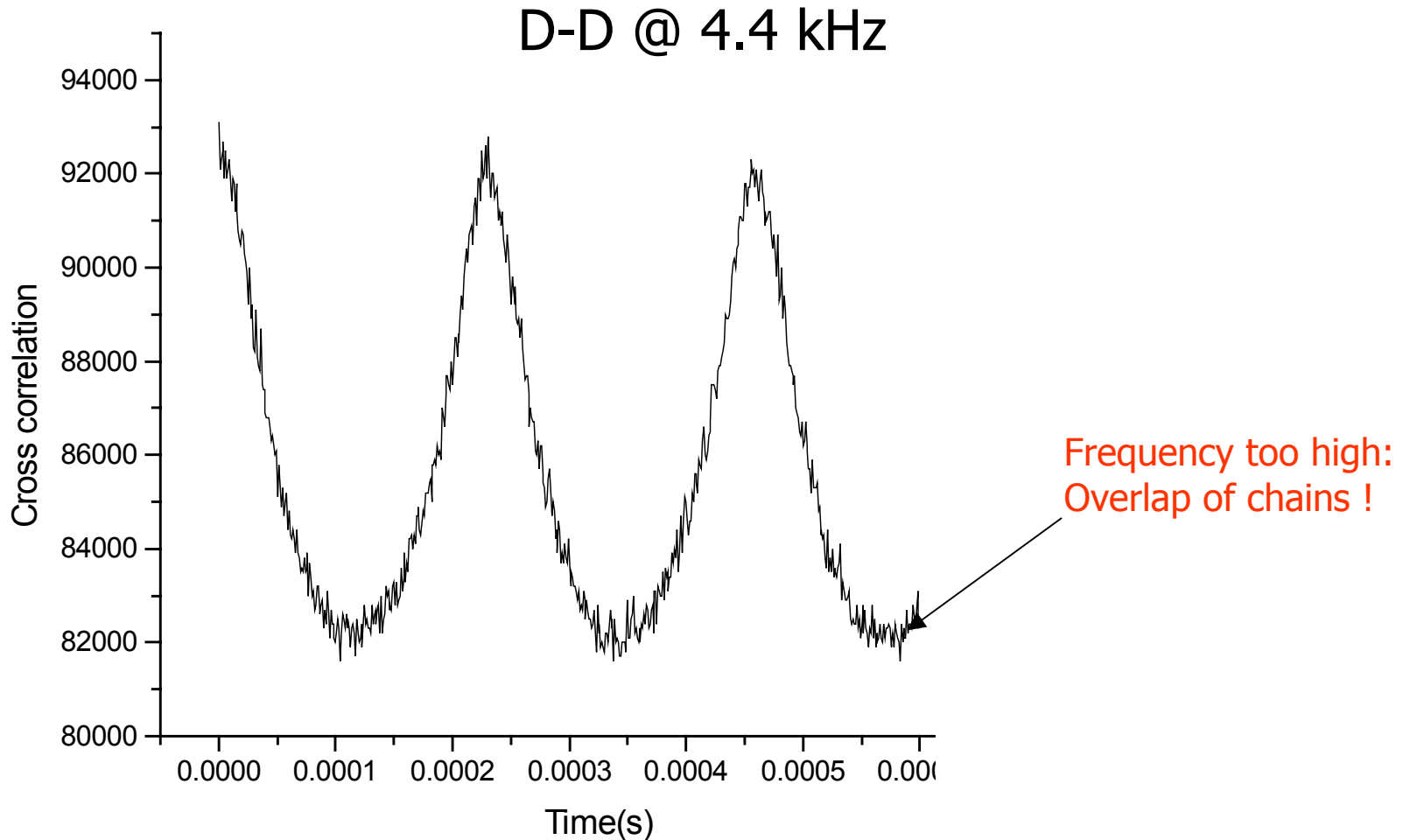


# Correlation results $\approx 1.5\%$ subcritical

D-D @ 1 kHz

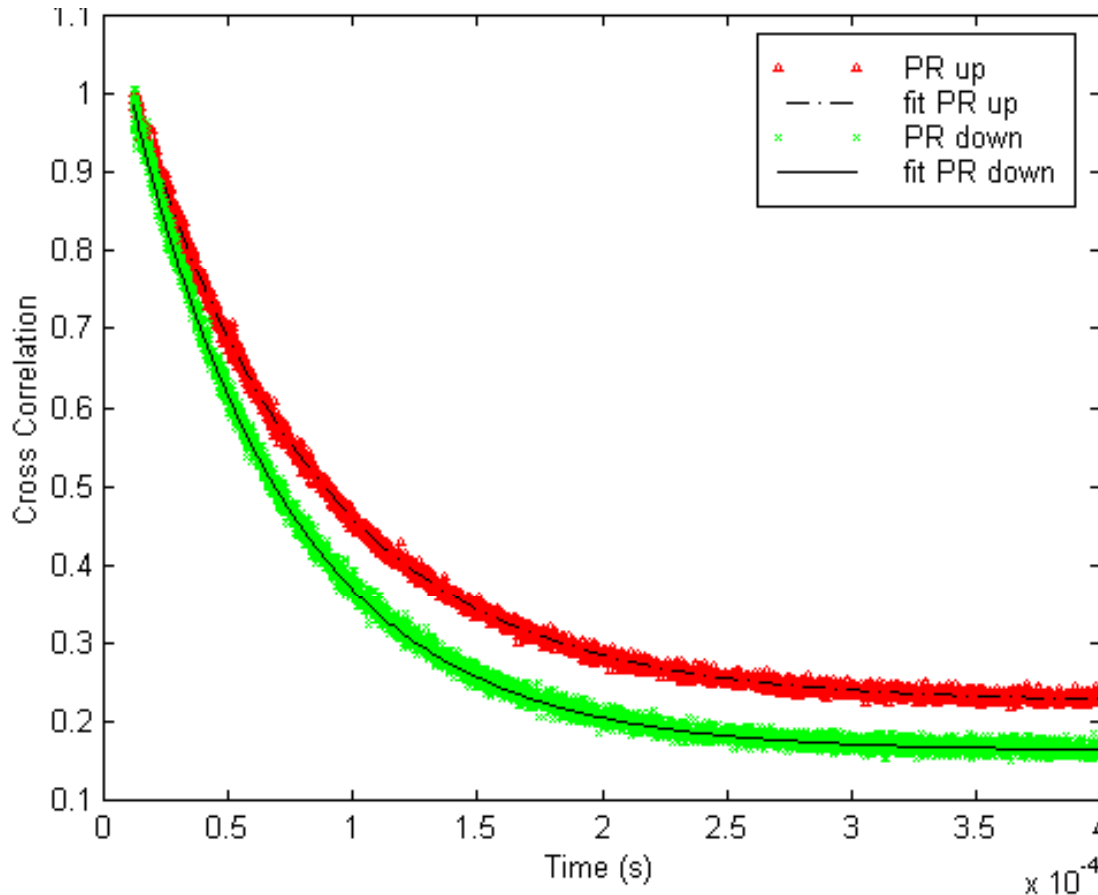


# Correlation results $\approx 1.5\%$ subcritical



# Correlation results $\approx 1.5\%$ subcritical

D-T @ 1 kHz



Pilot rod out:

$$\alpha = 15752 \text{ rad.s}^{-1}$$

$$(\rho = -588 \text{ pcm})$$

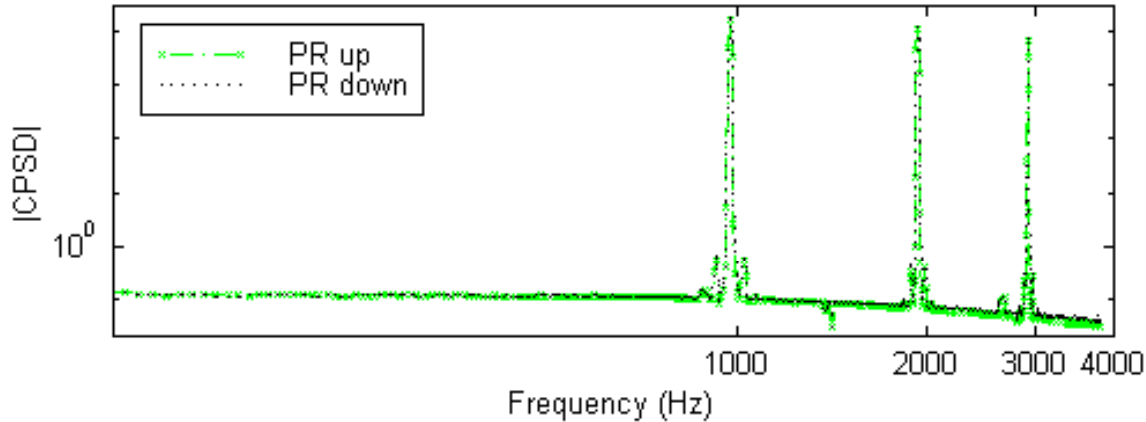
Pilot rod in:

$$\alpha = 13598 \text{ rad.s}^{-1}$$

$$(\rho = -462 \text{ pcm})$$

# CPSD results $\approx 1.5\%$ subcritical

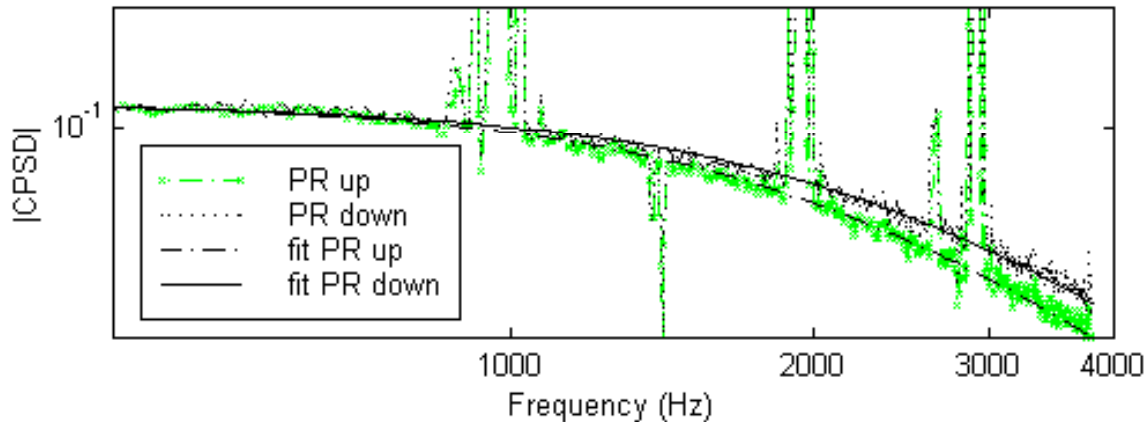
D-T @ 1 kHz



Pilot rod out:

$$\alpha = 16023 \text{ rad}\cdot\text{s}^{-1}$$

$$(\rho = -604 \text{ pcm})$$



Pilot rod in:

$$\alpha = 13930 \text{ rad}\cdot\text{s}^{-1}$$

$$(\rho = -481 \text{ pcm})$$

# Conclusions and further work

- Modification to Feynman- $\alpha$  to correct for echoes successful
- Feynman- $\alpha$  values in agreement with correlation and others
- Experimental Feynman- $\alpha$  results for pulsed systems
- Cross-correlation and CPSD give very fast accurate results
- Needed to remove peaks from the CPSD before fitting
- Comparison with other experimental groups under way
- Analysis of measurements at other configurations (SC2)